## Easy Crypto

Getting in touch with cryptography

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LosFuzzy's Training Session

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Introduction

## Overview

We will look at some entry-level cryptography that is often used in hacklets to disguise flags.

## Caesar

## Sample text

## ILP CRWWV ZOVMQL QOXFKFKD

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- Every letter is shifted


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- If 26 letters are used: only 26 possibilities


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## ILP CRWWV ZOVMQL QOXFKFKD <br> JMQ DSXXW APWNRM RPYGLGLE

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- Brute force until we have meaningful text


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## ILP CRWWV ZOVMQL QOXFKFKD <br> JMQ DSXXW APWNRM RPYGLGLE <br> KNR ETYYX BQXOSN SQZHMHMF

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- Classic Caesar cipher
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- If 26 letters are used: only 26 possibilities
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## Substitution Cipher

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- Replace symbols in plaintext with different symbols


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- Higher complexity: polyalphabetic substitution cipher


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- Higher complexity: polyalphabetic substitution cipher
- One symbol is made of multiple letters


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- One symbol is one letter
- Each letter is replaced by a different letter
- Caesar cipher is a "systematic" monoalphabetic substitution cipher
- Higher complexity: polyalphabetic substitution cipher
- One symbol is made of multiple letters
- Vigenere cipher is a "systematic" polyalphabetic substitution cipher

Monoalphabetic substitution cipher

## Caesar

AX qgm IZafc UjqhIgYjShZq ak IZW SfkoWj Ig qgmj hjgTdWe, IZWf qgm Vgf2l cfgo oZSI qgmj hjgTdWe ak. FWmeSff, usst

## Caesar

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- More fun if the alphabet size is unknown


## Caesar

AX qgm IZafc UjqhIgYjShZq ak IZW SfkoWj Ig qgmj hjgTdWe, IZWf qgm Vgf2l cfgo oZSI qgmj hjgTdWe ak. FWmeSff, usst

- More fun if the alphabet size is unknown
- Still easy to brute force


## Caesar brute force - Code

```
upper = "".join([chr(ascii) for ascii in range(65,91)])
lower = "".join([chr(ascii) for ascii in range(97,123)])
digit = "".join([chr(ascii) for ascii in range(48,58)])
# select the alphabet: uppercase, lowercase, digits and apostrophe
ALPHABET = upper + lower + digit + "'"
# try all possible keys
KEY = range(Ien(ALPHABET))
# message to decode
MSG = "AX qgm IZafc UjqhIgYjShZq ak IZW SfkoWj Ig qgmj" +
    "hjgTdWe, IZWf qgm Vgf2l cfgo oZSI qgmj hjgTdWe ak. FWmeSff, usst"
for k in KEY:
    out = ""
    for c in MSG:
        try:
            out += ALPHABET[(ALPHABET.index(c) + k) % len(ALPHABET)]
        except:
            out += c
    print("%d: %s" % (k, out))
```


## Caesar brute force

0: AX qgm lZafc UjqhlgYjShZq ak lZW SfkoWj lg qgmj hjgTdWe, lZWf qgm Vgf 21 cfgo oZSl qgmj hjgTdWe ak. FWmeSff, usst 1: BY rhn mabgd VkrimhZkTiar bl maX TglpXk mh rhnk ikhUeXf, maXg rhn Whg3m dghp paTm rhnk ikhUeXf bl. GXnfTgg, vttu 2: CZ sio nbche WlsjnialUjbs cm nbY UhmqYl ni siol jliVfYg, nbYh sio Xih4n ehiq qbUn siol jliVfYg cm. HYogUhh, wuuv 3: Da tjp ocdif XmtkojbmVkct dn ocZ VinrZm oj tjpm kmjWgZh, ocZi tjp Yji5o fijr rcVo tjpm kmjWgZh dn. IZphVii, xvvw
4: Eb ukq pdejg YnulpkcnWldu eo pda Wjosan pk ukqn lnkXhai, pdaj ukq Zkj6p gjks sdWp ukqn lnkXhai eo. JaqiWjj, ywwx
5: Fc vlr qefkh ZovmqldoXmev fp qeb Xkptbo ql vlro molYibj, qebk vlr alk7q hklt teXq vlro molYibj fp. KbrjXkk, zxxy
6: Gd wms rfgli apwnrmepYnfw gq rfc Ylqucp rm wmsp npmZjck, rfcl wms bml8r ilmu ufYr wmsp npmZjck gq. LcskYll, Oyyz
7: He xnt sghmj bqxosnfqZogx hr sgd Zmrvdq sn xntq oqnakdl, sgdm xnt cnm9s jmnv vgZs xntq oqnakdl hr. MdtlZmm, $1 z z 0$
8: If you think cryptography is the answer to your problem, then you don't know what your problem is. Neumann, 2001
9: Jg zpv uijol dszquphsbqiz jt uif botxfs up zpvs qspcmfn, uifo zpv epoAu lopx xibu zpvs qspcmfn jt. Ofvnboo, 3112
10: Kh Oqw vjkpm et0rvqitcrj0 ku vjg cpuygt vq Oqwt rtqdngo, vjgp Oqw fqpBv mpqy yjcv Oqwt rtqdngo ku. Pgwocpp, 4223
11: Li $1 r x$ wklqn fulswrjudsk1 lv wkh dqvzhu wr 1rxu sureohp, wkhq $1 r x$ grqCw nqrz zkdw 1rxu sureohp lv. Qhxpdqq, 5334
12: Mj 2sy xlmro gv2txskvetl2 mw xli erw0iv xs 2syv tvsfpiq, xlir 2sy hsrDx ors0 0lex 2syv tvsfpiq mw. Riyqerr, 6445
13: Nk 3tz ymnsp hw3uytlwfum3 nx ymj fsx1jw yt 3tzw uwtgqjr, ymjs 3tz itsEy pst1 1mfy 3tzw uwtgqjr nx. Sjzrfss, 7556
14: Ol 4 u0 znotq ix $4 v z u m x g v n 4$ oy znk gty $2 k x$ zu $4 u 0 x$ vxuhrks, znkt $4 u 0$ jutFz qtu2 2ngz $4 u 0 x$ vxuhrks oy. Tk0sgtt, 8667
15: Pm 5v1 0opur jy5w0vnyhwo5 pz 0ol huz3ly 0v 5v1y wyvislt, 0olu $5 \mathrm{v} 1 \mathrm{kvuG0}$ ruv3 $30 h 05 \mathrm{v} 1 \mathrm{y}$ wyvislt pz. Ul1thuu, 9778
16: Qn 6w2 1pqvs kz6x1wozixp6 q0 1pm iv04mz 1w 6w2z xzwjtmu, 1pmv 6w2 lwvH1 svw4 4pi1 6w2z xzwjtmu q0. Vm2uivv, '889
17: Ro $7 x 3$ 2qrwt $107 y 2 x p 0 j y q 7$ r1 2qn jw15n0 $2 x 7 x 30$ y0xkunv, 2qnw $7 x 3$ mxwI2 twx5 $5 q j 27 x 30$ y0xkunv r1. Wn3vjww, A99'
18: Sp 8y4 3rsxu m18z3yq1kzr8 s2 3ro kx26o1 3y 8y41 z1ylvow, 3rox 8y4 nyxJ3 uxy6 6rk3 8y41 z1ylvow s2. Xo4wkxx, B' 'A
19: Tq 9z5 4styv n2904zr2l0s9 t3 4sp ly37p2 4z 9z52 02zmwpx, 4spy 9z5 ozyK4 vyz7 7sl4 9z52 02zmwpx t3. Yp5xlyy, CAAB
20: Ur '06 5tuzw o3'150s3m1t' u4 5tq mz48q3 50 '063 130nxqy, 5tqz '06 p0zL5 wz08 8tm5 '063 130nxqy u4. Zq6ymzz, DBBC

## Complexer cipher

## Good news everyone


we are done with brute force

## Substitution cipher

WSie ueScADSGf
j bHcf heSifSD i hNNB YeScSGfifANG ONe fsS zNc mHIIkc. uBSicS OAGD Af iffihsSD fN fsAc StiAB. j
SGhekYfSD Af EAfs iSc HcAGR i 128-KAf qSk RSGSeifSD HcAGR fsS eiGD() OHGhfang NO fsS h cfiGDieD BAKeiek. PNfS fsif j hNtYABSD fsS qSk fndik if 12:00it. jG iDDAfANG fN fsAc YeScSGfifang, j iDDSD iG iefAhBS iKNHf iG AGfSeScfagr hekYfn-iBRNeAfst. LNESQSe, AG NeDSe fN eSid fsS iefAhBS (Af Ac iYYeNwAtifSBk 3500 hsieihfSec BNGR), kNH GSSD fN eSQSecS Esif j DAD fN sADS Af'c hNGfSGf OeNt kNH.
j RAQS kNH i sAGf: ZNH’BB GSSD fsS sSBY NO i
OitNHc eNtiG StYSeNe.
lsSSec, xBAhS

## Substitution cipher - Most frequent letter $\mathbf{S}$ to e

Weie ueecADeGf
j bHcf heeifeD i hNNB YeeceGfifANG ONe fse zNc mHIIkc. uBeice OAGD Af iffihseD fN fsAc etiAB. j
eGhekYfed Af EAfs iec HcAGR i 128-KAf qek ReGeeifeD HcAGR fse eiGD() OHGhfANG NO fse h cfiGDieD BAKeiek. PNfe fsif j hNtYABeD fse qek fNDik if 12:00it.
jG iDDAfANG fN fsAc YeeceGfifANG, j iDDeD iG iefAhBe iKNHf iG AGfeeecfAGR hekYfN-iBRNeAfst. LNEeQee, AG NeDee fN eeiD fse iefAhBe (Af Ac iYYeNwAtifeBk 3500 hsieihfeec BNGR), kNH GeeD fN eeQeece Esif j DAD fN sADe Af'c hNGfeGf OeNt kNH.
j RAQe kNH i sAGf: ZNH’BB GeeD fse seBY NO i
OitNHc eNtiG etYeeNe.
lseeec, xBAhe

## Substitution cipher - Guess words

Weie ueecADeGf
j bHcf heeifeD i hNNB YeeceGfifANG ONe fse zNc mHIIkc. uBeice OAGD Af iffihseD fN fsAc etiAB. j
eGhekYfed Af EAfs iec HcAGR i 128-KAf qek ReGeeifeD HcAGR fse eiGD() OHGhfANG NO fse h cfiGDieD BAKeiek. PNfe fsif j hNtYABeD fse qek fNDik if 12:00it.
jG iDDAfANG fN fsAc YeeceGfifANG, j iDDeD iG iefAhBe iKNHf iG AGfeeecfagr hekYfN-iBRNeAfst. LNEeQee, AG NeDee $f N$ eeiD fse iefAhBe (Af Ac iYYeNwAtifeBk 3500 hsieihfeec BNGR), kNH GeeD fN eeQeece Esif j DAD fN sADe Af'c hNGfegf OeNt kNH.
j RAQe kNH i sAGf: ZNH’BB GeeD fse seBY NO i
OitNHc eNtiG etYeeNe.
lseeec, xBAhe

## Substitution cipher - Guess words

Weir uresADeGf
j bHsf hreifeD i hNNB YreseGfifANG ONr fhe zNs mHIIks. uBeise OAGD Af iffihheD fN fhAs etiAB. j eGhrkYfeD Af EAfh ies HsAGR i 128-KAf qek ReGerifeD HsAGR fhe riGD() OHGhfANG NO fhe $h$ sfiGDirD BAKrirk. PNfe fhif j hNtYABeD fhe qek fNDik if 12:00it.
jG iDDAfANG fN fhAs YreseGfifANG, j iDDeD iG irfAhBe iKNHf iG AGferesfAGR hrkYfN-iBRNrAfht. LNEeQer, AG NrDer fN reiD fhe irfAhBe (Af As iYYrNwAtifeBk 3500 hhirihfers BNGR), kNH GeeD fN reQerse Ehif j DAD fN hADe Af's hNGfeGf OrNt kNH. j RAQe kNH i hAGf: ZNH'BB GeeD fhe heBY NO i OitNHs rNtiG etYerNr. cheers, xBAhe

## Substitution cipher - Guess words

Weir uresADeGf
j bHsf hreifeD i hNNB YreseGfifANG ONr fhe zNs mHIIks. uBeise OAGD Af iffihheD fN fhAs etiAB. j eGhrkYfeD Af EAfh ies HsAGR i 128-KAf qek ReGerifeD HsAGR fhe riGD() OHGhfANG NO fhe $h$ sfiGDirD BAKrirk. PNfe fhif j hNtYABeD fhe qek fNDik if 12:00it.
jG iDDAfANG fN fhAs YreseGfifANG, j iDDeD iG irfAhBe iKNHf iG AGferesfAGR hrkYfN-iBRNrAfht. LNEeQer, AG NrDer fN reiD fhe irfAhBe (Af As iYYrNwAtifeBk 3500 hhirihfers BNGR), kNH GeeD fN reQerse Ehif j DAD fN hADe Af's hNGfeGf OrNt kNH. j RAQe kNH i hAGf: ZNH'BB GeeD fhe heBY NO i OitNHs rNtiG etYerNr. cheers, xBAhe

## Substitution cipher - Guess words

Weir uresADeGt
j bHst hreiteD i hNNB YreseGtitANG ONr the zNs mHIIks. uBeise OAGD At ittihheD tN thAs etiAB. j eGhrkYteD At EAth ies HsAGR i 128-KAt qek ReGeriteD HsAGR the riGD() OHGhtANG NO the $h$ stiGDirD BAKrirk. PNte thit j hNtYABeD the qek tNDik it 12:00it.
jG iDDAtANG tN thAs YreseGtitANG, j iDDeD iG irtAhBe iKNHt iG AGterestAGR hrkYtN-iBRNrAtht. LNEeQer, AG NrDer tN reiD the irtAhBe (At As iYYrNwAtiteBk 3500 hhirihters BNGR), kNH GeeD tN reQerse Ehit j DAD tN hADe At's hNGteGt OrNt kNH. j RAQe kNH i hAGt: ZNH'BB GeeD the heBY NO i OitNHs rNtiG etYerNr.
cheers, xBAhe

## Substitution cipher - Guess words

Weir uresiDeGt
j bHst hreiteD i hNNB YreseGtitiNG ONr the zNs mHIIks. uBeise OiGD it ittihheD tN this etiiB. j eGhrkYteD it Eith ies HsiGR i 128-Kit qek ReGeriteD HsiGR the riGD() OHGhtiNG NO the $h$ stiGDirD BiKrirk. PNte thit j hNtYiBeD the qek tNDik it 12:00it.
jG iDDitiNG tN this YreseGtitiNG, j iDDeD iG irtihBe iKNHt iG iGterestiGR hrkYtN-iBRNritht. LNEeQer, iG NrDer tN reiD the irtihBe (it is iYYrNwititeBk 3500 hhirihters BNGR), kNH GeeD tN reQerse Ehit j DiD tN hiDe it's hNGteGt OrNt kNH.
j RiQe kNH i hiGt: ZNH'BB GeeD the heBY NO i OitNHs rNtiG etYerNr.
cheers, xBihe

## Substitution cipher - Guess words

Weir uresiDeGt
j bHst hreiteD i hNNB YreseGtitiNG ONr the zNs mHIIks. uBeise OiGD it ittihheD tN this etiiB. j eGhrkYteD it Eith ies HsiGR i 128-Kit qek ReGeriteD HsiGR the riGD() OHGhtiNG NO the $h$ stiGDirD BiKrirk. PNte thit j hNtYiBeD the qek tNDik it 12:00it.
jG iDDitiNG tN this YreseGtitiNG, j iDDeD iG irtihBe iKNHt iG iGterestiGR hrkYtN-iBRNritht. LNEeQer, iG NrDer tN reiD the irtihBe (it is iYYrNwititeBk 3500 hhirihters BNGR), kNH GeeD tN reQerse Ehit j DiD tN hiDe it's hNGteGt OrNt kNH.
j RiQe kNH i hiGt: ZNH'BB GeeD the heBY NO i OitNHs rNtiG etYerNr.
cheers, xBihe

## Substitution cipher - Guess words

Weir uresiDent
j bHst hreiteD i hNNB YresentitiNn ONr the zNs mHIIks. uBeise OinD it ittihheD tN this etiiB. j enhrkYteD it Eith ies Hsing i 128-Kit qek generiteD Hsing the rinD() OHnhtiNn NO the $h$ stinDirD BiKrirk. PNte thit j hNtYiBeD the qek tNDik it 12:00it.
jn iDDitiNn tN this YresentitiNn, j iDDeD in irtihBe iKNHt in interesting hrkYtN-iBgNritht. LNEeQer, in NrDer tN reiD the irtihBe (it is iYYrNwititeBk 3500 hhirihters BNng), kNH neeD tN reQerse Ehit j DiD tN hiDe it's hNntent OrNt kNH. j giQe kNH i hint: ZNH'BB neeD the heBY NO i OitNHs rNtin etYerNr. cheers, xBihe

## Substitution cipher - Guess words

Weir uresiDent
j bHst hreiteD i hNNB YresentitiNn ONr the zNs mHIIks. uBeise OinD it ittihheD tN this etiiB. j enhrkYteD it Eith ies Hsing i 128-Kit qek generiteD Hsing the rinD() OHnhtiNn NO the $h$ stinDirD BiKrirk. PNte thit j hNtYiBeD the qek tNDik it 12:00it.
jn iDDitiNn tN this YresentitiNn, j iDDeD in irtihBe iKNHt in interesting hrkYtN-iBgNritht. LNEeQer, in NrDer tN reiD the irtihBe (it is iYYrNwititeBk 3500 hhirihters BNng), kNH neeD tN reQerse Ehit j DiD tN hiDe it's hNntent OrNt kNH. j giQe kNH i hint: ZNH'BB neeD the heBY NO i OitNHs rNtin etYerNr. cheers, xBihe

## Substitution cipher - Guess words

Wear uresiDent
j bHst hreateD a hooB presentation Oor the zos mHIIks. uBease OinD it attahheD to this etaiB. j enhrkpteD it Eith aes Hsing a 128-Kit qek generateD Hsing the ranD() OHnhtion oO the $h$ stanDarD BiKrark. Pote that $j$ hotpiBeD the qek toDak at 12:00at. jn aDDition to this presentation, $j$ aDDeD an artihBe aKoHt an interesting hrkpto-aBgoritht. LoEeQer, in orDer to reaD the artihBe (it is approwitateBk 3500 hharahters Bong), koH neeD to reQerse Ehat j DiD to hiDe it's hontent Orot koH.
j giQe koH a hint: ZoH'BB neeD the heBp oO a
OatoHs rotan etperor.
cheers, xBihe

## Substitution cipher - Guess words

Wear uresiDent
j bHst hreateD a hooB presentation Oor the zos mHIIks. uBease OinD it attahheD to this etaiB. j enhrkpteD it Eith aes Hsing a 128-Kit qek generateD Hsing the ranD() OHnhtion oO the $h$ stanDarD BiKrark. Pote that $j$ hotpiBeD the qek toDak at 12:00at. jn aDDition to this presentation, $j$ aDDeD an artihBe aKoHt an interesting hrkpto-aBgoritht. LoEeQer, in orDer to reaD the artihBe (it is approwitateBk 3500 hharahters Bong), koH neeD to reQerse Ehat j DiD to hiDe it's hontent Orot koH. j giQe koH a hint: ZoH'BB neeD the heBp oO a OatoHs rotan etperor. cheers, xBihe

## Substitution cipher - Guess words

Wear uresident
j bHst hreated a hooB presentation Oor the zos mHIIks. uBease Oind it attahhed to this etaiB. j enhrkpted it Eith aes Hsing a 128-Kit qek generated Hsing the rand() OHnhtion oO the $h$ standard BiKrark. Pote that $j$ hotpiBed the qek todak at 12:00at. jn addition to this presentation, $j$ added an artihBe aKoHt an interesting hrkpto-aBgoritht. LoEeQer, in order to read the artihBe (it is approwitateBk 3500 hharahters Bong), koH need to reQerse Ehat j did to hide it's hontent Orot koH.
j giQe koH a hint: ZoH'BB need the heBp oO a
OatoHs rotan etperor.
cheers, xBihe

## Substitution cipher - Guess words

Wear uresident
j bHst hreated a hooB presentation Oor the zos mHIIks. uBease Oind it attahhed to this etaiB. j enhrkpted it Eith aes Hsing a 128-Kit qek generated Hsing the rand() OHnhtion oO the $h$ standard BiKrark. Pote that $j$ hotpiBed the qek todak at 12:00at.
jn addition to this presentation, $j$ added an artihBe aKoHt an interesting hrkpto-aBgoritht. LoEeQer, in order to read the artihBe (it is approwitateBk 3500 hharahters Bong), koH need to reQerse Ehat j did to hide it's hontent Orot koH. j giQe koH a hint: ZoH'BB need the heBp oO a OatoHs rotan etperor. cheers, xBihe

## Substitution cipher - Guess words

Dear uresident
I bust created a cool presentation for the zos muIIys. ulease find it attached to this email. I encrypted it with aes using a 128-Kit qey generated using the rand() function of the c standard liKrary. Note that I compiled the qey today at 12:00am.
In addition to this presentation, I added an article aKout an interesting crypto-algorithm. LoweQer, in order to read the article (it is approwimately 3500 characters long), you need to reQerse what I did to hide it's content from you. I giQe you a hint: Zou'll need the help of a famous roman emperor.
cheers, xlice

## Substitution cipher - Guess words

Dear President
I just created a cool presentation for the Los Fuzzys. Please find it attached to this email. I encrypted it with aes using a 128-bit key generated using the rand() function of the c standard library. Note that I compiled the key today at 12:00am.
In addition to this presentation, I added an article about an interesting crypto-algorithm. However, in order to read the article (it is approximately 3500 characters long), you need to reverse what I did to hide it's content from you. I give you a hint: You'll need the help of a famous roman emperor.
Cheers, Alice


Vigenère

## Vigenère

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## Vigenère

Vigenère

- Polyalphabetic substitution cipher


## Vigenère

Vigenère

- Polyalphabetic substitution cipher
- Composed of multiple Caesar ciphers


## Vigenère

Vigenère

- Polyalphabetic substitution cipher
- Composed of multiple Caesar ciphers
- Uses a keyword to select the Caesar shift


## LOS FUZZYS

| L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M | N | O | P | Q | R | S | T | U | V | W | $\times$ | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L |
| N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M |
| O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N |
| P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O |
| Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P |
| R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q |
| S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R |
| T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S |
| U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T |
| V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

## LOS FUZZYS

## K

| A | B | C | D | E | F | G | H | I | J | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | F | G | H | I | J | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | K | L | M | N | O | P | Q | R | S | T | U | V | W | $X$ | Y | Z | A | B | C | D | E | F | G | H |  |
| K | L | M | N | O | P | Q | R | S | T | U | V | W | X | $Y$ | Z | A | B | C | D | E | F | G | H | 1 | $J$ |
| L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K |
| M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L |
| N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M |
| O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N |
| P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O |
| Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P |
| R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q |
| S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R |
| T | U | V | W | X | Y | Z | A | B | C | D | E | $F$ | G | H | 1 | J | K | L | M | N | O | P | Q | R | S |
| U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T |
| V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

## LOS FUZZYS

K

| A | B | C | D | E | $F$ | G | H | I | J | K | L | M | N | O | P | Q | R | 5 | T | U | $V$ | W | X | Y | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S |  | U | V | W | X | Y | Z | A |
| C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | $V$ | W | X | Y | Z | A | B |
| D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | $V$ | W | X | Y | Z | A | B | C |
| E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | G | H | 1 | J | K | L | M | N | $\bigcirc$ | P | Q | R | S | T | U | V | W | $X$ | Y | Z | A | B | C | D | E |
| G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | 1 | J | K | L | M | N | O | P | Q | R | S | 1 | U | V | W | $X$ | Y | Z | A | B | C | D | E | F | G |
| 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 |
| K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |  | D | E |  | G | H |  | J |
| L | M | N | O | P | Q | R | S | T | U | $V$ | W | X | Y | Z | A | B | C | D |  |  | G | H |  | J | K |
| M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |  |  | G | H |  | J | K | L |
| N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |  |  | G | H |  | J | K | L | M |
| $\bigcirc$ | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |  | G | H |  | J | K | L | M | N |
| P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  | J | K | L | M | N | 0 |
| Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  | J | K | L | M | N | 0 | P |
| R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  | J | K | L | M | N | O | P | Q |
| S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R |
| T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S |
| U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T |
| V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | 0 | P | Q | R | S | T | U | V |
| X | Y | Z | A | B | C | D | E | $F$ | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | 1 | U | $V$ | W | X |
| Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

## LOS FUZZYS

## 1

| A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B | C | D | E | $F$ | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | D | E | F | G | H | 1 | J | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | $V$ | W | X | Y | Z | A | B | C |
| E | $F$ | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | H | 1 | J | K | L | M | N | O | P | Q | R | 5 | T | U | V | W | X | Y | 2 | A | B | C | D | E | F |
| H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | $F$ | G |
| 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 |
| K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J |
| L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K |
| M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  | J | K | L |
| N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M |
| O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N |
| P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  | J | K | L | M | N | O |
| Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | 0 | P |
| R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  | J | K | L | M | N | O | P | Q |
| S | T | U | V | W | $X$ | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R |
| T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S |
| U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T |
| V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | $P$ | Q | R | S | T | U | V | W | X |
| Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

$\qquad$

## LOS FUZZYS

## K

| A | B | C | D | E | F | G | H |  | J | K | L | M | N | O | P | Q | R | S | T | U | $V$ | W | X | Y | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B | C | D | E | F | G | H |  | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | $V$ | , | X | Y | Z | A | B |
| D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |  | Y | Z | A | B | C |
| E | F | G | H | 1 | J | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X |  | Z | A | B | C | D |
| F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | $V$ | W | X | Y | Z | A | B | C | D | E |
| G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  |
| K | L | M | N | O | P | Q | R | S | T | U | $V$ | W | X | Y | Z | A | B | C | D | E | F | G | H |  | J |
| L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |  | G | H |  | J | K |
| M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  | J | K | L |
| N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |  |  | J | K | L | M |
| O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  | J | K | L | M | N |
| P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  |  | K | L |  | N | O |
| Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J |  | L | M | N | O | P |
| R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q |
| S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R |
| T | U | $V$ | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S |
| U | $V$ | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | $J$ | K | L | M | N | 0 | P | Q | R | S | T |
| V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | 5 | T | U | V | V | X |
| Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

VSQ PY _---

## LOS FUZZYS

## K

| A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | $P$ | Q | R | S | T | U | V | W | X | Y | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | $Q$ | R | S | T | U | V | W | X | Y | Z | A |
| C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | 1 | U | V | W | X | Y | Z | A | B |
| D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | $E$ |
| G | H | I | J | K | L | M | N | O | P | $Q$ | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | $F$ |
| H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | K | L | M | N | $\bigcirc$ | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  |
| K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J |
| L | M | N | $\bigcirc$ | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K |
| M | N | O | P | Q | R | S | T | U | V | W | X | $Y$ | Z | A | B | C | D | E | F | G | H | 1 | J | K | L |
| N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M |
| $\bigcirc$ | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N |
| P | Q | R | S | T | U | V | W | X | $Y$ | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | $\bigcirc$ |
| Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | $P$ |
| R | S | T | U | V | W | X | Y | Z | A | B | C | D | $E$ | F | G | H | 1 | J | K | L | M | N | O | P | $Q$ |
| S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | $R$ |
| T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | $\bigcirc$ | P | Q | R | S | T |
| V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | $Q$ | R | S | T | U | V |
| X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | $Q$ | R | S | T | U | V | W |
| Y | Z | A | B | C | D | $E$ | $F$ | G | H | 1 | J | K | L | M | N | $\bigcirc$ | P | $Q$ | R | S | T | U | V | W | $X$ |
| Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | $R$ | S | T | U | V | W | X | $Y$ |

## VSQ PYX

## LOS FUZZYS

|  | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
|  | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
|  | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
|  | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
|  | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
|  | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
|  | H | 1 | $J$ | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
|  | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
|  | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 |
|  | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J |
|  | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
|  | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L |
|  | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M |
| $Y$ | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | $F$ | G | H | 1 | J | K | L | M | N |
|  | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
|  | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P |
|  | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q |
|  | S | T | U | V | W | X | Y | Z | A | B | C | D | E | $F$ | G | H | 1 | J | K | L | M | N | O | P | Q | R |
|  | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S |
|  | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | 0 | P | Q | R | S | T |
|  | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U |
|  | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V |
|  | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
|  | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | $X$ |
|  | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

VSQ PYXJ_-

## LOS FUZZYS

## K

| A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | D | E | F | G | H | 1 | J | K | L | M | N | O | $P$ | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | E | F | G | H | I | J | K | L | M | N | O | P | $Q$ | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | F | G | H | 1 | J | K | L | M | N | $\bigcirc$ | P | $Q$ | $R$ | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | G | H | I | J | K | L | M | N | $\bigcirc$ | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| 1 | J | K | L | M | N | $\bigcirc$ | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 |
| K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |  | J |
| L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K |
| M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L |
| N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M |
| O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N |
| P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | $\bigcirc$ | P |
| R | S | T | U | V | W | X | Y | Z | A | B | C | D | $E$ | F | G | H |  | J | K | L | M | N | O | P | Q |
| S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R |
| T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S |
| U | V | W | X | $Y$ | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T |
| V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | Y | Z | A | B | C | D | E | F | G | H | 1 | $J$ | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Z | A | B | C | D | $E$ | F | G | H | 1 | J | K | L | M | N | O | P | $Q$ | $R$ | S | T | U | V | W | X |
| Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

VSQ PYXJC

## LOS FUZZYS

| A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | $P$ | Q | R | S | T | U | V | W | X | Y | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | $Q$ | R | S | T | U | V | W | X | Y | Z | A |
| C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | $R$ | S | T | U | V | W | X | $Y$ | Z | A | B |
| D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | F | G | H | 1 | J | K | L | M | N | $\bigcirc$ | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | G | H | 1 | J | K | L | M | N | O | P | $Q$ | R | S | T | U | V | W | $X$ | Y | Z | A | B | C | D | $E$ |
| G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 |
| K | L | M | N | $\bigcirc$ | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J |
| L | M | N | $\bigcirc$ | P | Q | $R$ | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K |
| M | N | $\bigcirc$ | P | Q | $R$ | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L |
| N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M |
| O | P | $Q$ | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N |
| P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O |
| Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P |
| R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q |
| S | T | U | V | W | $X$ | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R |
| T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | $Q$ | R | S |
| U | V | W | X | $Y$ | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T |
| V | W | X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | X | Y | Z | A | B | C | D | $E$ | F | G | H | 1 | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | $R$ | S | T | U | V | W |
| Y | Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | $\bigcirc$ | P | $Q$ | R | S | T | U | V | W | X |
| Z | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | O | P | Q | $R$ | S | T | U | V | W | X | Y |

## VSQ PYXJCQ

## How to break

- Finding the key length using the Kasiski examination:


## How to break

- Finding the key length using the Kasiski examination:
- Find same words


## How to break

- Finding the key length using the Kasiski examination:
- Find same words
- Note the difference in their text position


## How to break

- Finding the key length using the Kasiski examination:
- Find same words
- Note the difference in their text position
- Factor all differences


## How to break

- Finding the key length using the Kasiski examination:
- Find same words
- Note the difference in their text position
- Factor all differences
- The factor that occurs most often is probably the key length


## Kasiski examination

myx iyhe,
h gcflc xmz qzmr yi ings or zli gzjc xild kthdx. rt gzjc xoqd wto zqc xohsygfd emw ngd htv vd ufhs sm ryds wto. cn wto jmmb ngd ajhsqyq jzqi xnzsgth? zqc dit ztfckzzqy nm kthczw scmdrjymsf, xyudl ug? okcfmd lypy rtpj snt bth's cpfq zsrjhshms nn xmzlrdjk qghjj snt'pj qzhrnhf emw or. vynn nm y gymbf fn okyyznqk xyudl, by vhjq zhmb dit sfjld. emqfnv sx omnzyltrgaykx!
yx nghq jgzhj nm rspthfkw jhbqwundc $g$ hum optphcc dit vgyb lnpj
cmemwgzsgth: ntp yuqfcy qhkj gy sgc sushmsuk ayse ne ufmghllnnm. rmy okys cr sm fnszap xtqgsa ktlhb shkj vdbyzmd lyss dlnqixdcx qhkj gy ntr yujhll ngdgw ftmam cm sfj ldrrfoqzlym hm rmy mdglbanpminc. uj uqd etcmf rt ord rmy azap ymspfhbd ysx adffpd kgpy rtnufhdpx ie emtx. nmaj qd zpj cm sfj vthjicmf uj qhkj zmd nsw wnucw nn fcy wknqj nn sfj wdmrwuk uyzfs. hr nm oqmyybsci vx rcayqzj lozqbx umc y mcfgjd mnofnmshafndc jfmsdp xsrscr. nn jltwj nsy ngd ezuqcq by vhjq ord amfnqmkiql. rt vqhll ngd kthdx mzn ne rmy azlp qd vgqf trc $f$ znnb ylnkjd. qd bys xhrazmr dtjlxsfnhf djxy nm kthczw! ho, anz

## Kasiski examination

myx iyhe,
h gcflc xmz qzmr yi ings or zli gzjc xild kthdx. rt gzjc xoqd wto zqc xohsygfd emw ngd htv vd ufhs sm ryds wto. cn wto jmmb ngd ajhsqyq jzqi xnzsgth? zqc dit ztfckzzqy nm kthczw scmdrjymsf, xyudl ug? okcfmd lypy rtpj snt bth's cpfq zsrjhshms nn xmzlrdjk qghjj snt'pj qzhrnhf emw or. vynn nm y gymbf fn okyyznqk xyudl, by vhjq zhmb dit sfjld. emqfnv sx omnzyltrgaykx!
yx nghq jgzhj nm rspthfkw jhbqwundc $g$ hum optphcc dit vgyb lnpj
cmemwgzsgth: ntp yuqfcy qhkj gy sgc sushmsuk ayse ne ufmghllnnm. rmy okys cr sm fnszap xtqgsa ktlhb shkj vdbyzmd lyss dlnqixdcx qhkj gy ntr yujhll ngdgw ftmam cm sfj ldrrfoqzlym hm rmy mdglbanpminc. uj uqd etcmf rt ord rmy azap ymspfhbd ysx adffpd kgpy rtnufhdpx ie emtx. nmaj qd zpj cm sfj vthjicmf uj qhkj zmd nsw wnucw nn fcy wknqj nn sfj wdmrwuk uyzfs. hr nm oqmyybsci vx rcayqzj lozqbx umc y mcfgjd mnofnmshafndc jfmsdp xsrscr. nn jltwj nsy ngd ezuqcq by vhjq ord amfnqmkiql. rt vqhll ngd kthdx mzn ne rmy azlp qd vgqf trc $f$ znnb ylnkjd. qd bys xhrazmr dtjlxsfnhf djxy nm kthczw! ho, anz

## Kasiski examination

myx iyhe,
h gcflc xmz qzmr yi ings or zli gzjc xild kthdx. rt gzjc xoqd wto zqc xohsygfd emw ngd htv vd ufhs sm ryds wto. cn wto jmmb ngd ajhsqyq jzqi xnzsgth? zqc dit ztfckzzqy nm kthczw scmdrjymsf, xyudl ug? okcfmd lypy rtpj snt bth's cpfq zsrjhshms nn xmzlrdjk qghjj snt'pj qzhrnhf emw or. vynn nm y gymbf fn okyyznqk xyudl, by vhjq zhmb dit sfjld. emqfnv sx omnzyltrgaykx!
yx nghq jgzhj nm rspthfkw jhbqwundc $g$ hum optphcc dit vgyb lnpj
cmemwgzsgth: ntp yuqfcy qhkj gy sgc sushmsuk ayse ne ufmghllnnm. rmy okys cr sm fnszap xtqgsa ktlhb shkj vdbyzmd lyss dlnqixdcx qhkj gy ntr yujhll ngdgw ftmam cm sfj ldrrfoqzlym hm rmy mdglbanpminc. uj uqd etcmf rt ord rmy azap ymspfhbd ysx adffpd kgpy rtnufhdpx ie emtx. nmaj qd zpj cm sfj vthjicmf uj qhkj zmd nsw wnucw nn fcy wknqj nn sfj wdmrwuk uyzfs. hr nm oqmyybsci vx rcayqzj lozqbx umc y mcfgjd mnofnmshafndc jfmsdp xsrscr. nn jltwj nsy ngd ezuqcq by vhjq ord amfnqmkiql. rt vqhll ngd kthdx mzn ne rmy azlp qd vgqf trc $f$ znnb ylnkjd. qd bys xhrazmr dtjlxsfnhf djxy nm kthczw! ho, anz

## Kasiski examination

myx iyhe,
h gcflc xmz qzmr yi ings or zli gzjc xild kthdx. rt gzjc xoqd wto zqc xohsygfd emw ngd htv vd ufhs sm ryds wto. cn wto jmmb ngd ajhsqyq jzqi xnzsgth? zqc dit ztfckzzqy nm kthczw scmdrjymsf, xyudl ug? okcfmd lypy rtpj snt bth's cpfq zsrjhshms nn xmzlrdjk qghjj snt'pj qzhrnhf emw or. vynn nm y gymbf fn okyyznqk xyudl, by vhjq zhmb dit sfjld. emqfnv sx omnzyltrgaykx!
yx nghq jgzhj nm rspthfkw jhbqwundc $g$ hum optphcc dit vgyb lnpj
cmemwgzsgth: ntp yuqfcy qhkj gy sgc sushmsuk ayse ne ufmghllnnm. rmy okys cr sm fnszap xtqgsa ktlhb shkj vdbyzmd lyss dlnqixdcx qhkj gy ntr yujhll ngdgw ftmam cm sfj ldrrfoqzlym hm rmy mdglbanpminc. uj uqd etcmf rt ord rmy azap ymspfhbd ysx adffpd kgpy rtnufhdpx ie emtx. nmaj qd zpj cm sfj vthjicmf uj qhkj zmd nsw wnucw nn fcy wknqj nn sfj wdmrwuk uyzfs. hr nm oqmyybsci vx rcayqzj lozqbx umc y mcfgjd mnofnmshafndc jfmsdp xsrscr. nn jltwj nsy ngd ezuqcq by vhjq ord amfnqmkiql. rt vqhll ngd kthdx mzn ne rmy azlp qd vgqf trc $f$ znnb ylnkjd. qd bys xhrazmr dtjlxsfnhf djxy nm kthczw! ho, anz

## Kasiski examination

myx iyhe,
h gcflc xmz qzmr yi ings or zli gzjc xild kthdx. rt gzjc xoqd wto zqc xohsygfd emw ngd htv vd ufhs sm ryds wto. cn wto jmmb ngd ajhsqyq jzqi xnzsgth? zqc dit ztfckzzqy nm kthczw scmdrjymsf, xyudl ug? okcfmd lypy rtpj snt bth's cpfq zsrjhshms nn xmzlrdjk qghjj snt'pj qzhrnhf emw or. vynn nm y gymbf fn okyyznqk xyudl, by vhjq zhmb dit sfjld. emqfnv sx omnzyltrgaykx!
yx nghq jgzhj nm rspthfkw jhbqwundc $g$ hum optphcc dit vgyb lnpj
cmemwgzsgth: ntp yuqfcy qhkj gy sgc sushmsuk ayse ne ufmghllnnm. rmy okys cr sm fnszap xtqgsa ktlhb shkj vdbyzmd lyss dlnqixdcx qhkj gy ntr yujhll ngdgw ftmam cm sfj ldrrfoqzlym hm rmy mdglbanpminc. uj uqd etcmf rt ord rmy azap ymspfhbd ysx adffpd kgpy rtnufhdpx ie emtx. nmaj qd zpj cm sfj vthjicmf uj qhkj zmd nsw wnucw nn fcy wknqj nn sfj wdmrwuk uyzfs. hr nm oqmyybsci vx rcayqzj lozqbx umc y mcfgjd mnofnmshafndc jfmsdp xsrscr. nn jltwj nsy ngd ezuqcq by vhjq ord amfnqmkiql. rt vqhll ngd kthdx mzn ne rmy azlp qd vgqf trc $f$ znnb ylnkjd. qd bys xhrazmr dtjlxsfnhf djxy nm kthczw! ho, anz

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- 5., 10., 15., ... letter is encrypted using a Caesar ciphers
- Use frequency analysis on each Caesar cipher


## Frequency analysis of first Caesar (1., 6., 11., ...)

- Most frequent letter: J


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- Guess that J equals $\mathbf{E}$ in original text


## Frequency analysis of first Caesar (1., 6., 11., ...)

- Most frequent letter: J
- Guess that J equals $\mathbf{E}$ in original text
- Looking at column $\mathbf{E}$ until we find J gives first letter of key: $\mathbf{F}$


## Frequency analysis of first Caesar (2., 7., 12., ...)

- Most frequent letter: $\mathbf{Y}$


## Frequency analysis of first Caesar (2., 7., 12., ...)

- Most frequent letter: $\mathbf{Y}$
- Guess that $\mathbf{Y}$ equals $\mathbf{E}$ in original text


## Frequency analysis of first Caesar (2., 7., 12., ...)

- Most frequent letter: $\mathbf{Y}$
- Guess that $\mathbf{Y}$ equals $\mathbf{E}$ in original text
- Looking at column $\mathbf{E}$ until we find $\mathbf{Y}$ gives second letter of key: $\mathbf{U}$


## Frequency analysis of first Caesar (3., 8., 13., ...)

- Most frequent letter: $\mathbf{N}$


## Frequency analysis of first Caesar (3., 8., 13., ...)

- Most frequent letter: $\mathbf{N}$
- Guess that $\mathbf{N}$ equals $\mathbf{E}$ in original text


## Frequency analysis of first Caesar (3., 8., 13., ...)

- Most frequent letter: $\mathbf{N}$
- Guess that $\mathbf{N}$ equals $\mathbf{E}$ in original text
- Looking at column $\mathbf{E}$ until we find $\mathbf{N}$ gives third letter of key: J


## Frequency analysis of first Caesar (4., 9., 14., ...)

- Most frequent letter: D


## Frequency analysis of first Caesar (4., 9., 14., ...)

- Most frequent letter: D
- Guess that $\mathbf{D}$ equals $\mathbf{E}$ in original text


## Frequency analysis of first Caesar (4., 9., 14., ...)

- Most frequent letter: D
- Guess that $\mathbf{D}$ equals $\mathbf{E}$ in original text
- Looking at column $\mathbf{E}$ until we find $\mathbf{D}$ gives fourth letter of key: $\mathbf{Z}$


## Frequency analysis of first Caesar (5., 10., 15., ...)

- Most frequent letters: $\mathbf{C}$ and $\mathbf{Y}$


## Frequency analysis of first Caesar (5., 10., 15., ...)

- Most frequent letters: $\mathbf{C}$ and $\mathbf{Y}$
- Guess that $\mathbf{C}$ or $\mathbf{Y}$ equals $\mathbf{E}$ in original text


## Frequency analysis of first Caesar (5., 10., 15., ...)

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- Guess that $\mathbf{C}$ or $\mathbf{Y}$ equals $\mathbf{E}$ in original text
- Looking at column $\mathbf{E}$ until we find $\mathbf{C}$ or $\mathbf{Y}$ gives fifth letter of key: $\mathbf{Y}$ or U


## Decrypting with key FUJZY

heo jack,
y heart you wqnt to zoin ui and mqke soce monuy. to mqke suhe you qre suytablu for txe job me wanj to meut you. to you anow txe cenjral pqrk stqtion? qre yok avaibable en montay nideteedth, selen pm? fleasu make iure yeu don'j draw qttenjion te yourielf wxile yeu're wqitinw for ui. wait en a bedch at flatferm selen, we mill fynd yok theru. follew us udobtrksiveby!
as txis emqil is itronwly ensryptud i cad provyde yok with core idformqtion: eur tahget wyll be jhe najionab bank ef wasxingten. the flan ii to atjack dkring bunch jime bucausu many umplooees wyll be eut taaing txeir lknch id the rustauhants yn the deighrorhoed. we ahe goidg to uie the rack edtranse and rehavu like iupplyers ov food. ence wu are id the bkildidg we wyll usu our cever te get cbose te the cuntrab vaulj. it is frotested bo sevehal guqrds add a hiwhly sephisjicatud lasjer syitem. te knoca out txe guahds we mill uie chlerofohm. to bhing txe monuy out ef the rank wu will kse a feod trelly. wu can dyscusi everothinw else en montay! cu, rob

## Fixing the key

- Looks already kind of readable


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- With the difference between $\mathbf{Q}$ and $\mathbf{A}$ we can correct the key
- J becomes Z
- The final key: FUZZY


## Decrypted text

hey jack,
i heard you want to join us and make some money. to make sure you are suitable for the job we want to meet you. do you know the central park station? are you available on monday nineteenth, seven pm? please make sure you don't draw attention to yourself while you're waiting for us. wait on a bench at platform seven, we will find you there. follow us unobtrusively!
as this email is strongly encrypted i can provide you with more information: our target will be the national bank of washington. the plan is to attack during lunch time because many employees will be out taking their lunch in the restaurants in the neighborhood. we are going to use the back entrance and behave like suppliers of food. once we are in the building we will use our cover to get close to the central vault. it is protected by several guards and a highly sophisticated laster system. to knock out the guards we will use chloroform. to bring the money out of the bank we will use a food trolly. we can discuss everything else on monday! cu, bob

## Questions?

## References

Caesar Cipher https://en.wikipedia.org/wiki/Caesar_cipher
Substitution Cipher https://en.wikipedia.org/wiki/Substitution_cipher
Frequency Analysis https://en.wikipedia.org/wiki/Frequency_analysis
Vigenère Cipher https://en.wikipedia.org/wiki/Vigen\�\�re_cipher
Kasiski examination https://en.wikipedia.org/wiki/Kasiski_examination

## ECDSA Hacklet

Breaking a secure signature scheme

Michael Schwarz
September 11, 2016
LosFuzzy's Training Session

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1. Introduction
2. The target
3. Elliptic Curves
4. ECDSA
5. Breaking into the server

Introduction

## Overview

We have to deal with a server storing notes where logins are based on strong elliptic curve cryptography (ECC): http://fuzzys.attacking.systems

We will analyze the used scheme, give an (ultra) short introduction to elliptic curves and then see how to break the scheme.

## The target

## The Server (i)

http://fuzzys.attacking.systems

## Secure Notice Board



Login

Download Signature Tool

## The Server (ii)

- The server has a list of users


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- Each user has a public key on the server


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- Each user has a public key on the server
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The scheme is based on ECDSA (Ellipctic Curve Digital Signature Algorithm)

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The scheme is based on ECDSA (Ellipctic Curve Digital Signature Algorithm)

1. Server displays a random nonce
2. User signs the nonce using his private key
3. User sends signed nonce (signature) to server
4. Server checks which public key verifies the signature
5. If there is a public key matching the signature, the server displays the notes of the corresponding user

## Network capture

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http://fuzzys.attacking.systems/dump.pcapng


## Elliptic Curves

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The set of points described by the following equation (Weierstrass normal form):

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y^{2}=x^{3}+a x+b
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We can add points two points $P$ and $Q$ on the curve

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## Note

This is a simplified representation - we will not cover any (mathematical) details and corner cases as this is not required to understand the signature algorithm.

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- It is the special case of the addition, where $P=Q$.
- The line between the two points is now the tangent to $P$



## Elliptic Curves - Scalar Multiplication ( $n \cdot P$ )

- We can multiply a point $P$ with a scalar ("normal number") $n$


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- These properties are the base of elliptic curve cryptography


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## How it works - Preparation

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- Alice sends Bob her public key $Q_{A}$


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- calculates the curve point $(r, y)=k \times G$
- calculates $s=k^{-1}\left(z+r d_{A}\right)$
- The signature is $(r, s)$


## How it works - Sign - Code

```
import hashlib, random, base64
from ecdsa import SigningKey
from ecdsa.util import string_to_number, sigencode_der
m = "Hi Bob!"
# read private key and curve parameters (d_A, G, ...)
sk = SigningKey.from_pem(open("signkey.pem").read())
# calculate z = hash(m)
z = string_to_number(hashlib.sha1(m).digest())
# random k
k = random.randint(0, sk. privkey.order)
# calculate r, s
r, s = sk.sign_number(z, None, k)
# encode signature
sig = sigencode_der(r, s, sk.privkey.order)
print(base64.b64encode(sig))
```

Breaking into the server

## Where is the vulnerability?

- The authentication scheme seems to be secure



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- The authentication scheme seems to be secure
- ECDSA is probably secure
- This is a crypto session, so maybe there is still something wrong with ECDSA...



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- Maybe some implementations do not comply to the standard


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Except for...

## Sony's ECDSA fail



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- And finally the private key $d_{A}=\frac{s k-z}{r}$


## Recover the private key - Code (1/2)

```
from ecdsa import SigningKey
from ecdsa.util import number_to_string, sigdecode_der
import base64, hashlib
# extended euclidean algorithm
def egcd(a, b):
    if a = 0:
            return (b, 0, 1)
    else:
            g, y, x = egcd(b % a, a)
            return (g, x - (b // a) * y, y)
# we cannot divide - have to multiply with modular inverse
def modinv(a, m):
    g, x, y = egcd(a,m)
    return x % m
# ensure values are not negative and in range [0, n)
def modn(val, n):
    while val < 0: val += n
    return val % n
# read our key for the curve parameters
sk = SigningKey.from_pem(open("user2_priv.pem").read ())
```


## Recover the private key - Code (2/2)

```
# captured nonces and signed nonces
nonce1 = b'iBW0oioDnq'
nonce2 = b'0CX9nTSLt2'
sign1 = base64.b64decode(
    b 'MDUCGQCPnWHAQc9Yiu0i0ZwYT6qe6YBVn0unZM4CGFQc2gBrmO4NInldykH1' +
    b 'PUUCPB53WutyBg==')
sign2 = base64.b64decode(
    b 'MDUCGQCPnWHAQc9Yiu0i0ZwYT6qe6YBVn0unZM4CGAYzHMi8TrvCJQxtMSmQ' +
    b'/u9+MVnZ+Jf8iQ==')
# get (r,s) and (r,s')
r1, s1 = sigdecode_der(sign1, sk.privkey.order)
r2, s2 = sigdecode_der(sign2, sk.privkey.order)
# calculate z and z'
z1 = int(hashlib.sha1(nonce1).hexdigest(), 16)
z2 = int(hashlib.sha1(nonce2).hexdigest(), 16)
# recover private key
n = sk.privkey.order
k = (modn(z1 - z2, n) * modinv(modn(s1 - s2, n), n)) % n
d}=(\operatorname{modn}(\textrm{s}1*\textrm{k}-\textrm{z}1,\textrm{n})*\operatorname{modinv}(\textrm{r}1,\textrm{n}))%\textrm{n
# show private key
sk_secret = SigningKey.from_string(number_to_string(d, n))
print(sk_secret.to_pem())
```


## Recover the private key

-----BEGIN EC PRIVATE KEY-----
MF8CAQEEGKjIYQURchpR7x7DGXSmTgQCv5PAJO+116AKBggqhkjOPQMBAaEOAzIA BEP05vGvGFRofftZj5zbIteDdqKGlt9KGDvQrxTQAT9X6/G++5h3AMyV3/M1Qv7r Qg==
-----END EC PRIVATE KEY-----


## Questions?

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- calculates the curve point $\left(x_{1}, y_{1}\right)=u_{1} \times G+u_{2} \times Q_{A}$
- The signature is valid if $x_{1} \equiv r$


## How it works - Verify - Code

```
from ecdsa import VerifyingKey
from ecdsa.util import sigdecode_der
# read public key and curve parameters (Q_A, G, ...)
vk = VerifyingKey.from_pem(open("verifykey.pem").read())
# sig = signature (DER encoded), m = message
print(vk.verify(sig, m, hashfunc=hashlib.sha1,
    sigdecode=sigdecode_der))
```


## References

[^1]
[^0]:    Source: http://cs.ucsb.edu/ koc/ccs130h/notes/ecdsa-cert.pdf

[^1]:    ECC http://andrea.corbellini.name/2015/05/17/elliptic-curve-cryptography-a-gentle-introduction/

    ECDSA https://en.wikipedia.org/wiki/Elliptic_Curve_Digital_Signature_Algorithm
    Python ECDSA https://github.com/warner/python-ecdsa
    Random Number https://xkcd.com/221/
    PS3 Hack https://events.ccc.de/congress/2010/Fahrplan/attachments/ 1780_27c3_console_hacking_2010.pdf

